

Combined 22xx and 23xx Key

Chemistry 271 – 22XX

Your Name: _____

Prof. Jason Kahn

University of Maryland, College Park

Your SID #: _____

General Chemistry and Energetics

Final Exam (200 points total)

Your Section # or time: _____

December 18, 2013

You have 120 minutes for this exam.

Explanations should be concise and clear. There is extra space on the last page if you need it.

You will need a calculator for this exam. No other study aids or materials are permitted.

Generous partial credit will be given, *i.e.*, if you don't know, guess.

Useful Equations:

$$K_a = [\text{H}^+][\text{A}^-]/[\text{HA}]$$

$$\text{pH} = -\log([\text{H}^+])$$

$$K_b = [\text{HA}][\text{HO}^-]/[\text{A}^-]$$

$$K_w = [\text{H}^+][\text{HO}^-]$$

$$\text{pH} = \text{p}K_a + \log [\text{A}^-]/[\text{HA}]$$

$$\Delta G^\circ = -RT \ln K_{eq}$$

$$R = 0.08206 \text{ L} \cdot \text{atm}/\text{mole K}$$

$$k_B = 1.38 \times 10^{-23} \text{ J/K}$$

$$\ln K_{eq} = -\Delta H^\circ/(RT) + \Delta S^\circ/R$$

$$\Delta S - q/T \geq 0$$

$$R = 8.314 \text{ J/mole K} = 1.987 \text{ cal/mole K} = N_A k_B$$

$$S = k_B \ln W$$

$$\Delta G = \Delta H - T\Delta S$$

$$\Delta G = \Delta G^\circ + RT \ln Q$$

Chemical standard state: 1 M solutes, pure liquids, 1 atm gases

Biochemical standard state: pH 7, all species in the ionic form found at pH 7

$$^\circ\text{C} = ^\circ\text{K} - 273.15$$

$$P(v)dv = Cv^2 \exp(-mv^2/2kT)$$

$$E = E^\circ - 2.303(RT/n\mathcal{F}) \log_{10} Q$$

$$2.303RT/\mathcal{F} = 0.0592 \text{ Volts at } 25^\circ\text{C}$$

$$\mathcal{F} = 96500 \text{ C (coulomb)}/\text{mole}$$

$$\Delta G^\circ = -n\mathcal{F}E^\circ_{\text{cell}}$$

$$\ln k = (-E_a/RT) + \ln A$$

$$1 \text{ Volt} = 1 \text{ Joule/Coulomb}$$

$$[\text{A}] = [\text{A}]_0 - kt$$

$$\ln[\text{A}] = \ln[\text{A}]_0 - kt$$

$$1/[\text{A}] = 1/[\text{A}]_0 + 2kt$$

Standard hydrogen electrode: $2 \text{H}^+(aq, 1 \text{ M}) + 2 e^- \rightarrow \text{H}_2(g)$ $E^\circ = 0.000 \text{ V}$

Honor Pledge: At the end of the examination time, please write out the following sentence and sign it, or talk to me about it:

"I pledge on my honor that I have not given or received any unauthorized assistance on this examination."

1. Short Answer (40 pts)

(a; 6 pts) Photosystem II in plants uses light energy to create a $P680^+$ cation that is a strong enough oxidizing agent to remove electrons from water, the product of which is the oxygen that we use to metabolize food we get from plants.

(b; 6 pts) Voltaic or Galvanic electrochemical cells use chemical energy to make electrical energy, whereas electrolytic cells use an external voltage to drive a/an non-spontaneous, uphill chemical change.

(c; 6 pts) Termolecular reactions in the gas phase are found when an inert collision gas is needed to remove energy from a pair of reacting partners that are forming a bond, which is (circle one) an exothermic/endothermic process.

(d; 6 pts) The Steady State Approximation applies to (circle one) reactants/intermediates/products that (circle all correct answers):

- + (a) accumulate to a high level during a reaction so that we can measure a steady concentration.
 + (b) are highly reactive so that they decay rapidly.
 + (c) are always present at vanishingly low concentrations.
 + (d) are created and destroyed at the same rate.

(e; 10 pts) True/False

Statement	T/F
Elementary reactions always get faster as temperature increases.	T
Equilibrium constants always increase as temperature increases	F
Rate laws can be written down by inspection if you know the equilibrium constant for a reaction	F
For a reaction $A \rightleftharpoons B$ where the molar free energies of A and B differ such that $G_A^\circ < G_B^\circ$, the minimum free energy state is a pure solution of A.	F
The minimum free energy state of the system corresponds to the minimum enthalpy state of the universe.	F

(f; 6 pts) An oxidizing agent with a standard reduction potential more positive than that of O_2 is thermodynamically unstable in the standard state because it will oxidize water to give O_2 .
 A reducing agent with E_{ox} more positive than that of H_2 is thermodynamically unstable because it will reduce protons to give H_2 .

1. Short Answer (40 pts)

(a; 6 pts) Photosystem I in plants uses light energy to create a P700* excited state that is a strong enough reducing agent (+2) to donate electrons (via intermediates) to NADP⁺ (+1) which gives NADPH (+1), which in turn ends up reducing CO₂ (+2) to make carbohydrates that we eat.

(b; 6 pts) Termolecular reactions in the gas phase are found when an inert collision gas is needed to remove energy (+2) from a pair of reacting partners that are forming (+2) a bond, which is (circle one) an exothermic (+2) endothermic process.

(c; 6 pts) Electrolysis (+2) electrochemical cells use an external voltage to drive a/an uphill / unfavorable / nonspontaneous (+2) chemical change, whereas galvanic or voltaic (+2) cells use chemical energy to make electrical energy.

(d; 6 pts) The Steady State Approximation applies to (circle one) reactants / intermediates / products that (circle all correct answers): +2

- +1 (a) are highly reactive so that they decay rapidly.
- +1 (b) accumulate to a high level during a reaction so that we can measure a steady concentration.
- +1 (c) are created and destroyed at the same rate.
- +1 (d) are always present at vanishingly low concentrations.

(e; 6 pts) An oxidizing agent with a standard reduction potential more positive than that of O₂ is (+3) thermodynamically unstable in the standard state because it will oxidize water to make O₂ (+3) in water. A reducing agent with E_{ox} more positive than that of H₂ is thermodynamically unstable because it will reduce H⁺ to make H₂ (+3).

(f; 10 pts) True/False

Statement	T/F
Elementary reactions always get slower as temperature decreases.	F (+1)
Rate laws cannot be written down by inspection unless you know the reaction is elementary.	T (+2)
Equilibrium constants always increase as temperature increases	F (+2)
The minimum free energy state of the system corresponds to the minimum enthalpy state of the universe.	F (+2)
For a reaction $A \rightleftharpoons B$ where the molar free energies of A and B differ such that $G_A^\circ < G_B^\circ$, the minimum free energy state is a pure solution of A.	F (+2)

2. Explanations (45 pts)

(a; 15 pts) Derive the Nernst equation using some of the equations on the front of the exam (equations that aren't the Nernst equation!). Conceptually explain why the sign must be negative in the Nernst equation.

$$(+3) \quad \Delta G = \Delta G^\circ + RT \ln Q$$

$$(+3) \quad \begin{cases} \Delta G^\circ = -n F E_{\text{cell}}^\circ \\ \Delta G = -n F E_{\text{cell}} \end{cases}$$

$$-n F E_{\text{cell}} = -n F E_{\text{cell}}^\circ + RT \ln Q$$

$$(+3) \quad E_{\text{cell}} = E_{\text{cell}}^\circ - \frac{RT}{nF} \cdot 2.303 \log_{10} Q$$

$$\frac{2.303 RT}{F} = 0.0592 \text{ V at } 25^\circ \text{C}$$

$$(+3) \quad E_{\text{cell}} = E_{\text{cell}}^\circ - \frac{0.0592}{n} \log_{10} Q$$

(+3) As $Q \uparrow$, ~~the~~ reaction becomes less favorable, so voltage drops - less energy per e^- .

(b; 15 pts) Briefly explain how increasing CO_2 levels in the atmosphere cause global warming, and mention one way in which society could attempt to return the atmosphere to 350 ppm.

(+5) - ~~CO₂~~ Visible light goes through the atmosphere and warms the earth, which gives off infrared radiation

(+5) - CO_2 absorbs IR and then re-emits it back down, warming the earth

(+5) - Hybrid cars, nuclear energy, CO_2 sequestration, global collapse of ~~all~~ air travel, biofuels, solar/wind/geothermal etc.

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(b; 15 pts) Derive the Nernst equation using some of the equations on the front of the exam (equations that aren't the Nernst equation!). Conceptually explain why the sign must be negative in the Nernst equation.

$$\begin{aligned}
 (+3) \quad \Delta G &= \Delta G^\circ + RT \ln Q \\
 (+3) \quad \Delta G^\circ &= -n F E^\circ_{\text{cell}} \\
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 \end{aligned}$$

$$-n F E_{\text{cell}} = -n F E^\circ_{\text{cell}} + RT \ln Q$$

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(+3) As $Q \uparrow$, ~~the~~ reaction becomes less favorable, so voltage drops - less energy per e⁻.

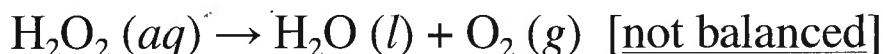
(15 pts) Explain why DNA hybridization reactions are typically carried out not far below the melting temperature of the desired double-stranded DNA product. In your answer, define the DNA melting temperature, mention mismatch thermodynamics, and speculate on hybridization kinetics.

- (+3) The melting temperature is T at which half of the DNA is in ss form and half is ds.
- (+4) The reaction is done near T_m to minimize the amount of mismatched/undesired hybridization, which is thermodynamically less stable ~~but~~ and \therefore melts at lower T_m (perfect match). Can't go above T_m because signal gets away.
- (+4) Also, the kinetics of hybridization are faster at high T -
- (+4) [mostly because marginally stable mismatches break up faster]

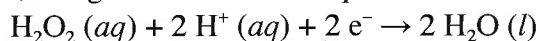
3. Electrochemistry and thermodynamics (55 pts)

There are several parts to this problem. They can frequently be answered even if you have not completed earlier parts.

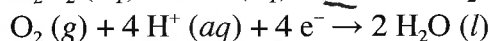
Hydrogen peroxide, H_2O_2 , is a moderately strong oxidizing agent. A H_2O_2 in aqueous solution is unstable, eventually decaying to give water and O_2 as follows:



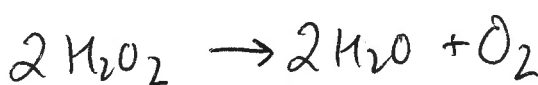
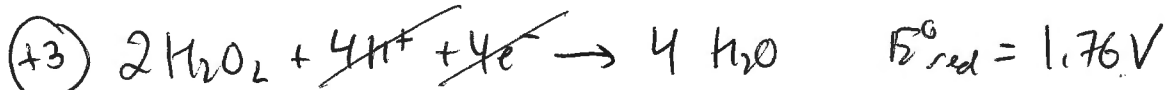
(a; 15 pts) Given the standard reduction potentials below, calculate E°_{cell} for the reaction above in acidic solution, and give the balanced equation for the overall reaction.



$$E^\circ_{\text{red}} = 1.76 \text{ V}$$



$$E^\circ_{\text{red}} = 1.23 \text{ V}$$



(+3)

$$E^\circ_{\text{cell}} = 1.76 - 1.23 \text{ V} = 0.53 \text{ V}$$

(+3)

(+3)

(b; 10 pts) Without doing a calculation, give E°_{cell} = the potential at pH 7 and also E°_{cell} under basic conditions, and explain your reasoning.

(+3) $E^{\circ}_{\text{cell}} = E^{\circ}_{\text{cell}} (\text{basic conditions}) = E^{\circ}_{\text{cell}} (\text{acidic}) = 0.53 \text{ V}$
(+3)

(+4) The overall reaction does not take up or liberate protons or hydroxide so the ΔG° and therefore E°_{cell} is independent of pH

(c; 30 pts) Calculate the standard state free energy change ΔG° for the H_2O_2 decay reaction under acidic conditions, at 298 K. Calculate the equilibrium constant for the reaction at 298 K. What would the concentration of H_2O_2 be at equilibrium with the air at $\text{PO}_2 = 0.21 \text{ atm}$? Why is a measurement of E°_{cell} a better way to measure this K_{eq} than attempting to measure the K_{eq} directly? Speculate on the sign of ΔS° . Does this tell you whether the equilibrium constant will go up or down as temperature increases?

(+2) $\Delta G^{\circ} = -n F E^{\circ}_{\text{cell}}$

(+3) $\Delta G^{\circ} = -4 \cdot 96500 \frac{\text{Coulombs}}{\text{mole}} \cdot 0.53 \frac{\text{Joules}}{\text{Coulomb}} = -204600 \text{ J/mole}$

(+2) $K_{\text{eq}} = e^{-\Delta G^{\circ}/RT}$
(+3) $K_{\text{eq}} = e^{+204600 / (8.314 \cdot 298 \text{ K})} = 7.26 \times 10^{35}$

(+3) $K_{\text{eq}} = \frac{\text{PO}_2 \cdot [\text{H}_2\text{O}]^2}{[\text{H}_2\text{O}_2]^2} = \frac{0.21}{[\text{H}_2\text{O}_2]^2}$

(+3) $[\text{H}_2\text{O}_2] = \sqrt{\frac{0.21}{7.26 \times 10^{35}}} = \sqrt{2.89 \times 10^{-37}} = 5.38 \times 10^{-19} \text{ M}$

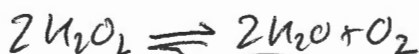
(+4) It would be extremely hard to measure 10^{-19} M - it would be about 30000 molecules in 20 ml. Much easier to measure a voltage.

(+3) ΔS° is probably positive because a molecule of gas is generated. But this does not tell us the sign of ΔH° (it's negative), so we don't know whether K_{eq} will increase or decrease.
(+2)
(+3)

(b; 10 pts) Without doing a calculation, give E°_{cell} = the potential at pH 7 and also E°_{cell} under basic conditions, and explain your reasoning.

(+3) $E^{\circ}_{\text{cell}} = E^{\circ}_{\text{cell}} (\text{basic condition}) = E^{\circ}_{\text{cell}} (\text{acidic}) = 0.53 \text{ V}$

(+4) The overall reaction does not have protons or hydroxide as a reactant or product, so E_{cell} is independent of pH.



(c; 30 pts) Calculate the standard state free energy change ΔG° for the H_2O_2 decay reaction under acidic conditions, at 298 K. Calculate the equilibrium constant for the reaction at 298 K. What would the concentration of H_2O_2 be at equilibrium with oxygen at $\text{PO}_2 = 0.65 \text{ atm}$? Why is a measurement of E°_{cell} a better way to measure this K_{eq} than attempting to measure the K_{eq} directly? Speculate on the sign of ΔS° . Does this tell you whether the equilibrium constant will go up or down as temperature increases?

(+2) $\Delta G^{\circ} = -n F E^{\circ}_{\text{cell}} = -4 \cdot 96500 \frac{\text{Coulombs}}{\text{mole}} \cdot 0.53 \frac{\text{Joules}}{\text{Coulomb}}$

(+3) $\Delta G^{\circ} = -204600 \text{ Joules/mole}$

(+2) $K_{\text{eq}} = e^{-\Delta G^{\circ}/RT} = e^{+204600 / (8.314 \cdot 298)} = 7.26 \times 10^{35}$
 or 55M okay, though wrong

(+3) $K_{\text{eq}} = \frac{\text{PO}_2 \cdot [\text{H}_2\text{O}]^2}{[\text{H}_2\text{O}_2]^2} = \frac{0.65}{[\text{H}_2\text{O}_2]^2} = 7.26 \times 10^{35}$

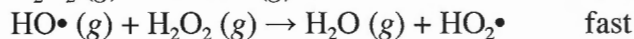
(+3) $[\text{H}_2\text{O}_2] = \sqrt{\frac{0.65}{7.26 \times 10^{35}}} = 9.46 \times 10^{-19} \text{ M}$

(+4) Such an infinitesimal concentration cannot be measured accurately, so it is much better to measure the voltage.

ΔS° is probably positive since gas is produced, but that doesn't tell you whether it is exothermic or not (it is), so no info on T-dependence of K .

4. Kinetics and Mechanism (60 pts)

The uncatalyzed breakdown of H_2O_2 is difficult to study, because the reaction is catalyzed in a wide variety of ways. The uncatalyzed reaction in the gas phase at high temperature is believed to occur through a series of steps, with the first step being a rate limiting unimolecular homolytic cleavage to give hydroxyl radical:



...

(a; 10 pts) Give the expected observed rate law for the breakdown of H_2O_2 . Also, explain how it is possible to ask you to do this even though I have not shown the rest of the mechanism.

ask you to do this even though I have not shown the rest of the mechanism.

Rate $= \frac{-1}{2} \frac{d[H_2O_2]}{dt} = k_1 [H_2O_2]$

OK to omit

(+3) for any rate law
(+3) for correct

OK to connect

(+4) Since step 1 is rate-limiting, all subsequent steps are kinetically invisible, except rate could be multiplied by a constant if the later rapid step already have H_2O_2 .

(b; 15 pts) The observed rate constant for this reaction has a preexponential factor of 10^{13} s^{-1} and an activation energy of 201000 J/mole . Calculate the rate constant at 400°C and at 100°C . What would the half-life be at 100°C for H_2O_2 at a concentration of 0.010 M ?

(f3) Arrhenius rate law -

hence rate law -
 $\ln k = -E_a/RT + \ln A$ so $k = Ae^{-E_a/RT}$

④3 $k = 10^{+13} \text{ s}^{-1} e^{-\frac{(201000 \text{ J/mol})}{(8.314 \cdot \underbrace{(400 + 273.15))}_{\text{K}}}} = 10^{+13} \text{ s}^{-1} e^{-35.91}$
 \downarrow
 unit van in first order ~~373~~ $= 2.53 \times 10^{-3} \text{ s}^{-1}$

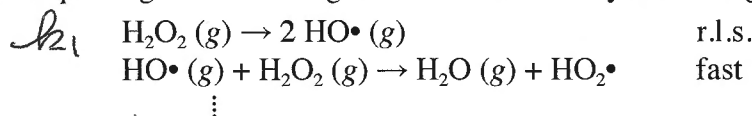
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(f3) At 100°C $k_2 = 10^{13} e^{-201600 / (8314 \cdot 373)} = 2.53 \times 10^{-5} \text{ s}^{-1}$
 ~~$= 10^{13} e^{-64.74} = 4.16 \times 10^{-14} \text{ s}^{-1}$~~
 $= 10^{13} e^{-64.81} = 7.10 \times 10^{-16}$

$$\begin{aligned} (t_3) t_{1/2} &= \ln 2 / k \quad \text{for 1st order} \\ &= \frac{0.693}{7.10 \times 10^{-16}} = 9.76 \times 10^{14} \text{ sec} \end{aligned}$$

4. Kinetics and Mechanism (60 pts)

The uncatalyzed breakdown of H_2O_2 is difficult to study, because the reaction is catalyzed in a wide variety of ways. The uncatalyzed reaction in the gas phase at high temperature is believed to occur through a series of steps, with the first step being a rate limiting unimolecular homolytic cleavage to give hydroxyl radical:



(a; 10 pts) Give the expected observed rate law for the breakdown of H_2O_2 . Also, explain how it is possible to ask you to do this even though I have not shown the rest of the mechanism.

Rate = $-\frac{1}{2} \frac{d[\text{H}_2\text{O}_2]}{dt} = k_1 [\text{H}_2\text{O}_2]$ (43) for any rate law (43) for correct don't need the "1/2"

If the first step is rate-limiting, none of the subsequent steps matter to the rate. [Although it could be $n \cdot k_1$ if the products lead to decay of n molecules of H_2O_2]

(b; 15 pts) The observed rate constant for this reaction has a preexponential factor of 10^{13} s^{-1} and an activation energy of 201000 J/mole. Calculate the rate constant at 500 °C and at 125 °C. What would the half-life be at 125 °C for H_2O_2 at a concentration of 0.020 M?

(43) Arrhenius rate law: $\ln k = \ln A - \frac{E_a}{RT}$ or $k = Ae^{-E_a/RT}$

(43) $k = 10^{13} \text{ s}^{-1} \cdot e^{(-201000 \text{ J/mole}) / (8.314 \text{ J/mole K} \cdot 773 \text{ K})}$

(43) $= 10^{13} \text{ s}^{-1} e^{-31.27} = 0.263 \text{ s}^{-1} @ 500^\circ\text{C}$

↳ hint that it's first order!

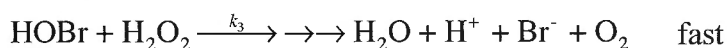
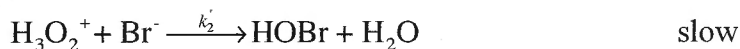
(43) $= 10^{13} \text{ s}^{-1} e^{-201000 / (8.314 \cdot 398 \text{ K})} = e^{-60.74} = 4.16 \times 10^{-27} \text{ s}^{-1} \text{ at } 398 \text{ K}$

(43) $t_{1/2} = \ln 2 / k$ for first order

$= 0.693 / (4.16 \times 10^{-27}) = 1.67 \times 10^{26} \text{ s} \approx 5 \times 10^8 \text{ years}$

$-\text{[H}_2\text{O}_2]$ is irrelevant.

You can buy hydrogen peroxide in aqueous solution, and it is reasonably stable on storage. However, there are many ways to catalyze the disproportionation. One example is the reaction with bromide ion under acidic conditions given by the proposed mechanism (= series of elementary reactions) below. The multiple arrows in the third step indicate fast steps that are kinetically invisible after an elementary S_N2 attack on HOBr (hypobromous acid) by H_2O_2 .



(c; 4 pts) Write down the rate of appearance of O_2 just according to the third line of the mechanism above.

To move further we will need the concentration of the reactive intermediate HOBr.

$$(+4) \quad \frac{d[O_2]}{dt} = k_3 [HOBr] [H_2O_2]$$

(d; 8 pts) Write down the expression for the rate of change of [HOBr] based on the 2nd and 3rd lines, and set the rate of change equal to zero (the SSA). Calculate the concentration of [HOBr]. Now you need to know the concentration of $H_3O_2^+$.

$$\frac{d[HOBr]}{dt} = k_2 [H_3O_2^+] [Br^-] - k_3 [HOBr] [H_2O_2] \stackrel{SSA}{=} 0 \quad (+2)$$

$$[HOBr] = \frac{k_2 [H_3O_2^+] [Br^-]}{k_3 [H_2O_2]} \quad (+3)$$

(e; 6 pts) Calculate $[H_3O_2^+]$ in terms of $[H_2O_2]$ and $[H^+]$ from the first line of the mechanism, assuming that $H_3O_2^+$ and H_2O_2 are in rapid equilibrium. Based on your knowledge of chemistry, why is this a reasonable assumption?

$$\textcircled{+3} \quad K_{eq} = \frac{k_1}{k_{-1}} = \frac{[H_3O_2^+]}{[H_2O_2][H^+]} \quad \text{so} \quad \frac{[H_3O_2^+]}{\textcircled{+2}} = \frac{k_1}{k_{-1}} [H_2O_2][H^+]$$

- ~~Assume~~ K_{eq} formation/decomposition is the fastest chemical reaction
 $\textcircled{+2}$

(f; 7 pts) Write down the overall differential rate law for the production of O_2 according to the mechanism given. Briefly, how could you test experimentally whether this rate law is correct? [You can answer the second part even if you didn't get the rate law].

$$\frac{d[O_2]}{dt} = k_3 [HOBr] [H_2O_2]$$

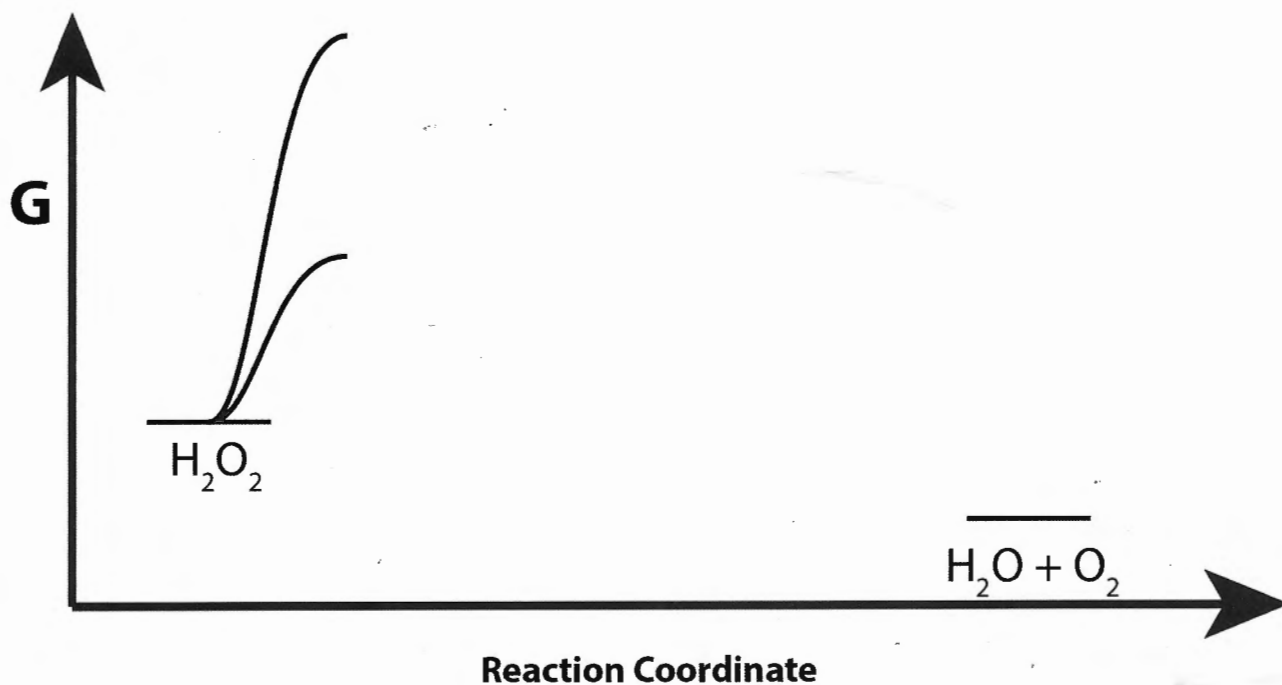
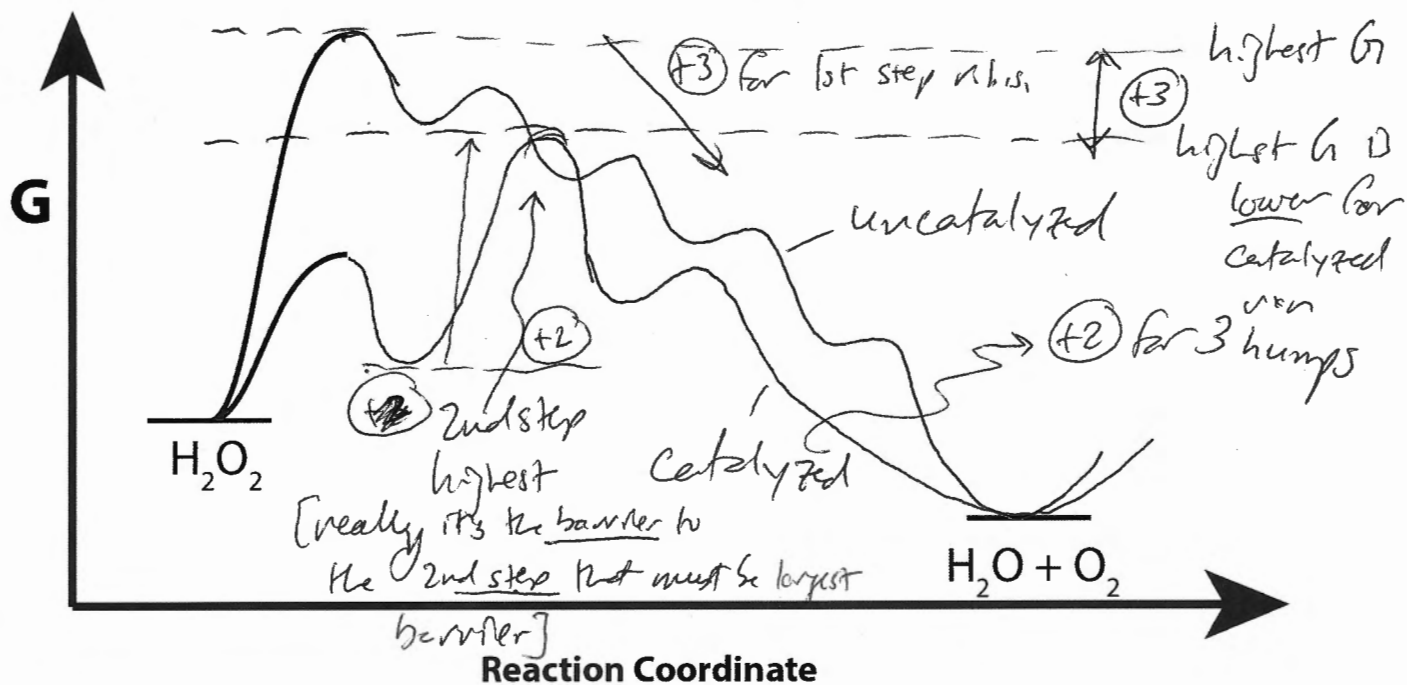
$\textcircled{+2}$ for any attempt at substitution $= k_3 \cdot \frac{k_2 [Br^-]}{k_3 [H_2O_2]} \cdot \frac{k_1}{k_{-1}} [H_2O_2][H^+] \cdot \cancel{[H_2O_2]}$

$$\frac{d[O_2]}{dt} = \frac{k_2 k_1}{k_{-1}} [Br^-] [H_2O_2] [H^+] \quad \textcircled{+2}$$

Reality check - k_3 doesn't matter ✓
 same as rapid pre-eg. result ✓

$\textcircled{+3}$ for either - Do the reaction at different $[Br^-]$, $[H_2O_2]$, and/or $[H^+]$ and measure initial rates
 - Curve-fitting to time course of reaction]

(g; 10 pts) Finally, complete the free energy reaction coordinate diagram comparing the uncatalyzed reaction (with its slow and rate-limiting first step) and the Br^- -catalyzed reaction. The graph is repeated in case you want to clean up your diagram. Indicate which one you want graded.



Score for the page_____

Extra work space. If you give an answer on this page make sure you write a clear note in the body of the exam telling us to look here.

Page	Score
2	/40
3	/30
4	/30
5	/40
6	/25
7	/12
8	/13
9	/10
Total	/200

Score for the page_____